

# Evidence of a new narrow resonance decaying to $\chi_{c1}\gamma$ in $B \rightarrow \chi_{c1}\gamma K$

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We report measurements of  $B \rightarrow \chi_{c1}\gamma K$  and  $\chi_{c2}\gamma K$  decays using  $772 \times 10^6$   $B\bar{B}$  events collected at the  $\Upsilon(4S)$  resonance with the Belle detector at the KEKB asymmetric-energy  $e^+e^-$  collider. Evidence of a new resonance in the  $\chi_{c1}\gamma$  final state is found with a statistical significance of  $3.8\sigma$ . This state has a mass of  $3823.1 \pm 1.8(\text{stat}) \pm 0.7(\text{syst})$  MeV/ $c^2$ , a value that is consistent with theoretical expectations for the previously unseen  $1^3D_2$   $c\bar{c}$  meson. We find no other narrow resonance and set upper limits on the branching fractions of the  $X(3872) \rightarrow \chi_{c1}\gamma$  and  $\chi_{c2}\gamma$  decays.

PACS numbers: 13.25.Hw, 13.20.Gd, 14.40.Pq

During the last decade, a number of new charmonium ( $c\bar{c}$ )-like states were observed, many of which are candidates for exotic states [1]. The first of these, the  $X(3872)$ , has been observed by six different experiments in the same final state [2–7]. A recent update from Belle [8] and LHCb [6] results in a world average mass at  $3871.68 \pm 0.17$  MeV/ $c^2$  [9] and a stringent upper bound on its width ( $\Gamma < 1.2$  MeV) [8]. The proximity of its mass to the  $D^{*0}\bar{D}^0$  threshold makes it a good candidate for a  $D\bar{D}^*$  molecule [10]. Other, but alternative models have been proposed, such as a tetraquark [11] or a  $c\bar{c}g$  hybrid me-

son [12].

Radiative decays can illuminate clearly the nature of hadrons. For example, the observation of  $X(3872) \rightarrow J/\psi\gamma$  confirmed the  $C$ -even parity assignment for the  $X(3872)$  [13, 14]. The similar decay mode  $X(3872) \rightarrow \psi'\gamma$  could help to distinguish whether the  $X(3872)$  is charmonium, a molecular state or a mixture of the two [10, 15, 16]. Belle reported no significant signal [14] in  $X(3872) \rightarrow \psi'\gamma$ , in disagreement with positive evidence from BaBar [13]. The  $X(3872) \rightarrow \chi_{c1}\gamma$  and  $\chi_{c2}\gamma$  decays are forbidden by  $C$ -parity conservation in electromag-

netic processes. However, if the  $X(3872)$  is a tetraquark or a molecular state, it may have a  $C$ -odd partner, which could decay into  $\chi_{c1}\gamma$  and  $\chi_{c2}\gamma$  final states [17, 18].

In the charmonium family, the observation of a  $D$ -wave  $c\bar{c}$  meson and its decay modes would test phenomenological models [19, 20]. The as-yet undiscovered  $1^3D_2$   $c\bar{c}$  ( $\psi_2$ ) and  $1^3D_3$   $c\bar{c}$  ( $\psi_3$ ) states are expected to have significant branching fractions to  $\chi_{c1}\gamma$  and  $\chi_{c2}\gamma$ , respectively [21, 22].  $D$ -wave  $c\bar{c}$  states and their properties were predicted long ago but remain unconfirmed [21, 22]. The E705 experiment reported an indication of a  $1^3D_2$  state in  $\pi^\pm N \rightarrow J/\psi \pi^+ \pi^- + \text{anything}$ , with a mass of  $3836 \pm 13$  MeV/ $c^2$  [23]; however, the statistical significance of this result was below the threshold for evidence.

In this letter, we report measurements of  $B \rightarrow \chi_{c1}\gamma K$  and  $B \rightarrow \chi_{c2}\gamma K$  decays, where the  $\chi_{c1}$  and  $\chi_{c2}$  decay to  $J/\psi\gamma$  [24]. These results are obtained from a data sample of  $772 \times 10^6$   $B\bar{B}$  events collected with the Belle detector [25] at the KEKB asymmetric-energy  $e^+e^-$  collider operating at the  $\Upsilon(4S)$  resonance [26]. The Belle detector is a large-solid-angle spectrometer, which includes a silicon vertex detector (SVD), a 50-layer central drift chamber (CDC), an array of aerogel threshold Cherenkov counters (ACC), time-of-flight scintillation counters (TOF), and an electromagnetic calorimeter (ECL) comprised of CsI(Tl) crystals located inside a superconducting solenoid coil that provides a 1.5 T magnetic field. An iron flux return located outside the coil is instrumented to detect  $K_L^0$  mesons and identify muons (KLM).

The  $J/\psi$  meson is reconstructed via its decays to  $\ell^+\ell^-$  ( $\ell = e$  or  $\mu$ ). To reduce the radiative tail in the  $e^+e^-$  mode, the four-momenta of all photons within 50 mrad with respect to the original direction of the  $e^+$  or  $e^-$  tracks are included in the invariant mass calculation, hereinafter denoted as  $M_{e^+e^-(\gamma)}$ . The reconstructed invariant mass of the  $J/\psi$  candidates is required to satisfy  $2.95$  GeV/ $c^2 < M_{e^+e^-(\gamma)} < 3.13$  GeV/ $c^2$  or  $3.03$  GeV/ $c^2 < M_{\mu^+\mu^-} < 3.13$  GeV/ $c^2$ . For the selected  $J/\psi$  candidates, a vertex-constrained fit is applied and then a mass-constrained fit is performed in order to improve the momentum resolution. The  $\chi_{c1}$  and  $\chi_{c2}$  candidates are reconstructed by combining  $J/\psi$  candidates with a photon having energy ( $E_\gamma$ ) larger than 200 MeV in the laboratory frame. Photons are reconstructed from the energy deposition in the ECL by requiring no matching with any extrapolated charged track. To reduce the background from  $\pi^0 \rightarrow \gamma\gamma$ , we use a likelihood function that distinguishes an isolated photon from  $\pi^0$  decays using the photon pair invariant mass, photon laboratory energy and polar angle [27]. We reject both  $\gamma$ 's in the pair if the  $\pi^0$  likelihood probability is larger than 0.7. The reconstructed invariant mass of the  $\chi_{c1}$  ( $\chi_{c2}$ ) is required to satisfy  $3.467$  GeV/ $c^2 < M_{J/\psi\gamma} < 3.535$  GeV/ $c^2$  ( $3.535$  GeV/ $c^2 < M_{J/\psi\gamma} < 3.611$  GeV/ $c^2$ ). A mass-constrained fit is applied to the selected  $\chi_{c1}$  and  $\chi_{c2}$  candidates.

Charged kaons are identified by combining information from the CDC, TOF, and ACC systems. The kaon identification efficiency is 89% while the probability of misidentifying a pion as a kaon is 10%.  $K_S^0$  mesons are reconstructed by combining two oppositely charged pions with the invariant mass  $M_{\pi^+\pi^-}$  lying between 482 MeV/ $c^2$  and 514 MeV/ $c^2$ . The selected candidates are required to satisfy the quality criteria described in Ref. [28].

To reconstruct  $B$  candidates, each  $\chi_{cJ}$  [29] is combined with a kaon candidate and a photon having  $E_\gamma > 100$  MeV (and not used in the reconstruction of  $\chi_{cJ}$ ). If the invariant mass of any photon pair that includes this photon is found to be consistent with a  $\pi^0$  (i.e.,  $117$  MeV/ $c^2 < M_{\gamma\gamma} < 153$  MeV/ $c^2$ ), this photon is rejected. Among the events containing at least one  $\chi_{cJ}$  candidate, 9.0% have multiple  $\chi_{cJ}$  candidates. In such cases, the  $\gamma$  forming the  $\chi_{cJ}$  candidate with mass closest to the  $\chi_{c1}$  or  $\chi_{c2}$  masses [9] is not used as the additional photon. This treatment suppresses reflections from the  $\chi_{cJ}$  daughter photons.

The  $B$  candidate is identified by two kinematic variables: the beam-constrained mass ( $M_{bc} \equiv \sqrt{E_{\text{beam}}^{*2} - p_B^{*2}}$ ) and the energy difference ( $\Delta E \equiv E_B^* - E_{\text{beam}}^*$ ). Here,  $E_{\text{beam}}^*$  is the run-dependent beam energy, and  $E_B^*$  and  $p_B^*$  are the reconstructed energy and momentum, respectively, of the  $B$  meson candidates in the center-of-mass (CM) frame. Candidates within a  $\Delta E$  window of  $[-28, 30]$  MeV and with  $M_{bc} > 5.23$  GeV/ $c^2$  are selected. Of these, 9.8% (6.4%) have multiple candidates in the  $B^\pm \rightarrow \chi_{c1}\gamma K^\pm$  ( $B^\pm \rightarrow \chi_{c2}\gamma K^\pm$ ) mode; we select the  $B$  candidate with  $\Delta E$  closest to zero. In order to improve the resolution in  $M_{\chi_{cJ}\gamma}$ , we scale the energy of the  $\gamma$  so that  $\Delta E$  is equal to zero. This corrects for incomplete energy measurement in the ECL. To suppress continuum background, events having a ratio  $R_2$  of the second to zeroth Fox-Wolfman moments [30] above 0.5 are rejected.

The  $M_{\chi_{c1}\gamma}$  and  $M_{bc}$  projections for the  $B^\pm \rightarrow \chi_{c1}\gamma K^\pm$  signal candidates are shown in Fig. 1, where a  $\psi' \rightarrow \chi_{c1}\gamma$  signal is evident. In addition, there is a significant narrow peak at 3823 MeV/ $c^2$ , denoted hereinafter as  $X(3823)$ . No signal of  $X(3872) \rightarrow \chi_{c1}\gamma$  is seen. We extract the signal yield from a two-dimensional unbinned extended maximum likelihood (2D UML) fit to the variables  $M_{\chi_{cJ}\gamma}$  and  $M_{bc}$ . The likelihood function is

$$\mathcal{L} = \frac{e^{-\sum_k n_k}}{N!} \prod_{i=1}^N \sum_k n_k P_k(m_{xi}, M_{bi}),$$

where  $k$  is the index for the signal and background contributions,  $n_k$  and  $P_k$  are the yield and probability density function (PDF), respectively, for the  $k$ -th component,  $m_{xi}$  and  $M_{bi}$  are the  $M_{\chi_{cJ}\gamma}$  and  $M_{bc}$  values in the  $i$ -th event, respectively, and  $N$  is the total number of candidate events in the data.

The resolution in  $M_{\chi_{cJ}\gamma}$  ( $M_{bc}$ ) is parameterized by a

sum of two Gaussians (Gaussian and logarithmic Gaussian [31]). MC studies show that the resolutions in both  $M_{\chi_{c1}\gamma}$  and  $M_{bc}$  for a narrow resonance in the mass range  $3.8 \text{ GeV}/c^2 < M_{\chi_{c1}\gamma} < 4.0 \text{ GeV}/c^2$  are in good agreement with those for  $\psi'$ . The parameters of the resolution functions are determined from the MC simulation that is calibrated using the  $B^\pm \rightarrow \psi'(\rightarrow \chi_{c1}\gamma)K^\pm$  signal. We take into account the  $\psi'$  natural width [9] by convolving the Breit-Wigner function and the resolution function; for the  $X(3823)$  and  $X(3872)$ , zero natural widths are assumed. The two-dimensional PDF is a product of the one-dimensional distributions.

For  $B^\pm \rightarrow \psi'(\rightarrow \chi_{c1}\gamma)K^\pm$  decay, the mean and width of the core Gaussian are floated and the remaining parameters are fixed according to MC. To fit the  $B^\pm \rightarrow X(3823)(\rightarrow \chi_{c1}\gamma)K^\pm$  signal, we float the mean of the core Gaussian but constrain the detector resolution by using the  $\psi'$  signal results after taking into account the difference estimated from the signal MC study. For  $M_{bc}$ , the parameters are fixed to those found for the  $\psi'$ , in accordance with expectations based on the MC simulation. We constrain the mass difference (from Ref. [9]) and the sigma difference (from MC simulations) between  $\psi'$  and  $X(3872)$ . To fit  $B^0 \rightarrow \psi'(\rightarrow \chi_{c1}\gamma)K^0$ ,  $B^0 \rightarrow X(3823)(\rightarrow \chi_{c1}\gamma)K^0$ ,  $B \rightarrow \psi'(\rightarrow \chi_{c2}\gamma)K$ ,  $B \rightarrow X(3823)(\rightarrow \chi_{c2}\gamma)K$  and  $B \rightarrow X(3872)(\rightarrow \chi_{c1}\gamma)K$ , we fix all the parameters obtained from the signal MC study after correcting the PDF shapes by applying MC/data calibration factors.

To study background with a real  $J/\psi$ , we use large MC simulated  $B \rightarrow J/\psi X$  samples corresponding to 100 times the integrated luminosity of the data. The non- $J/\psi$  (non- $\chi_{cJ}$ ) background is studied using  $M_{\ell\ell}$  ( $M_{J/\psi\gamma}$ ) sidebands in data. In the  $B \rightarrow (\chi_{cJ}\gamma)K$  cases, the background with a broad peaking structure is mostly due to the  $B \rightarrow \psi'(\rightarrow \chi_{cJ}\gamma)K$ ,  $B \rightarrow \chi_{cJ}K^*$ ,  $B \rightarrow J/\psi K^*$  and  $B \rightarrow \psi'K^*$  decay modes.  $B \rightarrow \psi'(\rightarrow \chi_{cJ}\gamma)K$  produces peaks in both distributions ( $M_{\chi_{cJ}\gamma}$  and  $M_{bc}$ ), while the other backgrounds are flat in  $M_{\chi_{cJ}\gamma}$  but peaked in  $M_{bc}$ . We determine the PDFs from the large MC sample. The fractions of the PDF components are floated in the fit, except for  $B \rightarrow \psi'(\rightarrow \chi_{cJ}\gamma)K$ , whose fraction is controlled by fixing its ratio to the  $B \rightarrow \psi'(\rightarrow \chi_{cJ}\gamma)K$  signal yield. For the combinatorial background, a threshold function,  $(M_{\chi_{cJ}\gamma})^2 \times \exp(a(M_{\chi_{cJ}\gamma} - M_{th}) + b(M_{\chi_{cJ}\gamma} - M_{th})^2 + c(M_{\chi_{cJ}\gamma} - M_{th})^3)$ , where  $M_{th} = 3.543 \text{ GeV}/c^2$  ( $3.585 \text{ GeV}/c^2$ ) for  $M_{\chi_{c1}\gamma}$  ( $M_{\chi_{c2}\gamma}$ ), is used for  $M_{\chi_{cJ}\gamma}$  and an ARGUS function [32] is used for  $M_{bc}$ . The value of  $M_{th}$  is estimated from a MC study; its variation, which affects the signal yield in the fits, is incorporated in the systematic errors. The  $\Delta E$  data sidebands are used to verify the background PDFs. The fractions for the signal and the background components are floated in the fit.

The results of the fits are presented in Figs. 1-3 and in Table I. The significance is estimated using the value of  $-2\ln(\mathcal{L}_0/\mathcal{L}_{\max})$  where  $\mathcal{L}_{\max}$  ( $\mathcal{L}_0$ ) denotes the likelihood value when the yield is allowed to vary (is set

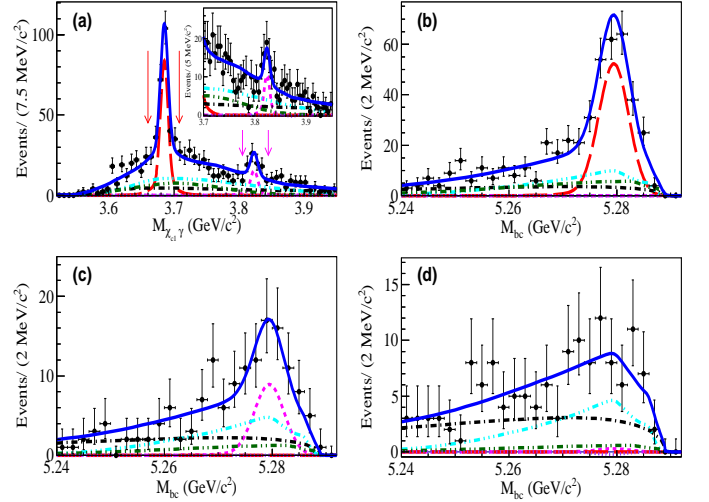


FIG. 1: 2D UML fit projection for  $B^\pm \rightarrow (\chi_{c1}\gamma)K^\pm$  decays: (a)  $M_{\chi_{c1}\gamma}$  distribution for  $M_{bc} > 5.27 \text{ GeV}/c^2$ , (b)  $M_{bc}$  distribution for  $3.660 \text{ GeV}/c^2 < M_{\chi_{c1}\gamma} < 3.708 \text{ GeV}/c^2$  ( $\psi'$  region, shown by red arrows), (c)  $M_{bc}$  distribution for  $3.805 \text{ GeV}/c^2 < M_{\chi_{c1}\gamma} < 3.845 \text{ GeV}/c^2$  ( $X(3823)$  region, shown by magenta arrows) and (d)  $M_{bc}$  distribution for  $3.84 \text{ GeV}/c^2 < M_{\chi_{c1}\gamma} < 3.89 \text{ GeV}/c^2$  ( $X(3872)$  region). The curves used in the fits are described in [33].

to zero). In the likelihood calculation, the  $\chi^2$  statistic uses the appropriate number of degrees of freedom (2 in case of  $B^\pm \rightarrow X(3823)K^\pm$  and 1 for the other decay modes). The systematic uncertainty, which is described below, is included in the significance calculation [34]. We find a significant  $\psi'$  signal in all considered channels. We also obtain evidence for the  $X(3823)$  in the channel  $B^\pm \rightarrow \chi_{c1}\gamma K^\pm$  with a statistical significance of 3.8 standard deviations ( $\sigma$ ). The  $X(3872)$  signals are insignificant. We estimate the branching fractions according to the formula  $\mathcal{B} = \frac{Y}{\epsilon \times \mathcal{B}_s \times N_{B\bar{B}}}$ ; here,  $Y$  is the yield,  $\epsilon$  is the reconstruction efficiency,  $\mathcal{B}_s$  is the secondary branching fractions taken from Ref. [9] and  $N_{B\bar{B}}$  is the number of the  $B\bar{B}$  mesons in the data sample. Equal production of neutral and charged  $B$  meson pairs in the  $\Upsilon(4S)$  decay is assumed. Measured branching fractions for the  $\psi'$  are in agreement with the world average values for all the channels [9]. We set 90% confidence level (C.L.) upper limits (U.L.) on the insignificant channels using frequentist methods based on an ensemble of pseudo-experiments.

A correction for small differences in the signal detection efficiency between MC and data has been applied for the lepton and kaon identification requirements. Uncertainties in these corrections are included in the systematic error. The  $\gamma\gamma \rightarrow \ell^+\ell^-$  and  $D^{*+} \rightarrow D^0(K^-\pi^+)\pi^+$  samples are used to estimate the lepton identification correction and the kaon (pion) identification correction, respectively. To estimate the correction and residual systematic uncertainty for  $K_S^0$  reconstruction,  $D^{*+} \rightarrow D^0(\rightarrow$



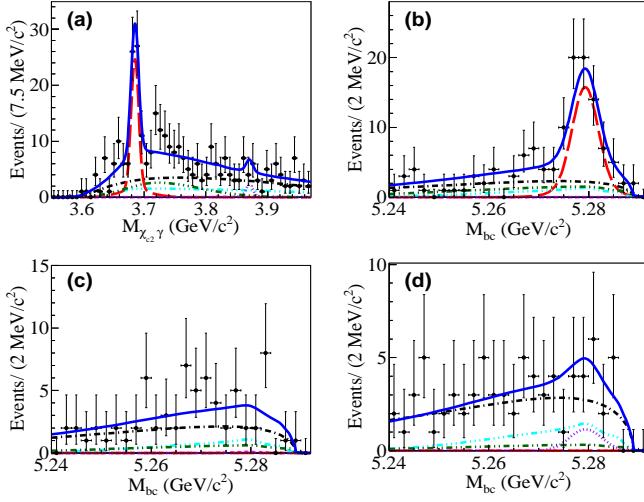


FIG. 2: 2D UML fit projection for  $B^\pm \rightarrow (\chi_{c2}\gamma)K^\pm$  decays: (a)  $M_{\chi_{c2}\gamma}$  distribution for  $M_{bc} > 5.27 \text{ GeV}/c^2$ , (b)  $M_{bc}$  distribution for  $3.660 \text{ GeV}/c^2 < M_{\chi_{c2}\gamma} < 3.708 \text{ GeV}/c^2$  ( $\psi'$  region), (c)  $M_{bc}$  distribution for  $3.805 \text{ GeV}/c^2 < M_{\chi_{c2}\gamma} < 3.845 \text{ GeV}/c^2$  ( $X(3823)$  region) and (d)  $M_{bc}$  distribution for  $3.84 \text{ GeV}/c^2 < M_{\chi_{c2}\gamma} < 3.89 \text{ GeV}/c^2$  ( $X(3872)$  region). The curves used in the fits are described in [33].

$K_S^0\pi^+\pi^-\pi^+$  samples are used. The errors on the PDF shapes are obtained by varying all fixed parameters by  $\pm 1\sigma$  and taking the change in the yield as the systematic uncertainty. The uncertainties due to the secondary branching fractions are also taken into account. The uncertainties of the tracking efficiency and  $N_{BB}$  are estimated to be 0.35% per track and 1.4%, respectively. The uncertainty on the photon identification is estimated to be 2.0%/photon. The systematic uncertainty associated with the difference of the  $\pi^0$  veto between data and MC is estimated to be 1.2% from a study of the  $B^\pm \rightarrow \chi_{c1}(\rightarrow J/\psi\gamma)K^\pm$  sample.

We also perform a simultaneous fit to  $B^\pm \rightarrow (\chi_{c1}\gamma)K^\pm$  and  $B^0 \rightarrow (\chi_{c1}\gamma)K_S^0$ , assuming that  $\mathcal{B}(B^\pm \rightarrow X(3823)K^\pm)/\mathcal{B}(B^0 \rightarrow X(3823)K^0) = \mathcal{B}(B^\pm \rightarrow \psi'K^\pm)/\mathcal{B}(B^0 \rightarrow \psi'K^0)$ . The  $\psi'$  peak position and  $M_{\chi_{c1}\gamma}$  resolution are common for both charged and neutral  $B$  candidates. From this fit, we estimate the significance for  $X(3823)$  to be  $4.0\sigma$  (including systematic uncertainties). We determine the mass of the signal peak relative to the well-measured  $\psi'$  mass :

$$M_{X(3823)} = M_{X(3823)}^{\text{meas}} - M_{\psi'}^{\text{meas}} + M_{\psi'}^{\text{PDG}} = 3823.1 \pm 1.8 \pm 0.7 \text{ MeV}.$$

Here, the first uncertainty is statistical and the second is systematic. Because of the mass-constrained fit to the  $\chi_{c1}\gamma$  candidate, the systematic uncertainty of  $M_{X(3823)}$  is dominated by the additional photon's energy scale. This photon energy scale uncertainty is estimated by the difference between the  $\chi_{c1} \rightarrow J/\psi\gamma$  candidates' mass without any constraint and the  $\chi_{c1}$  nominal mass [9], which

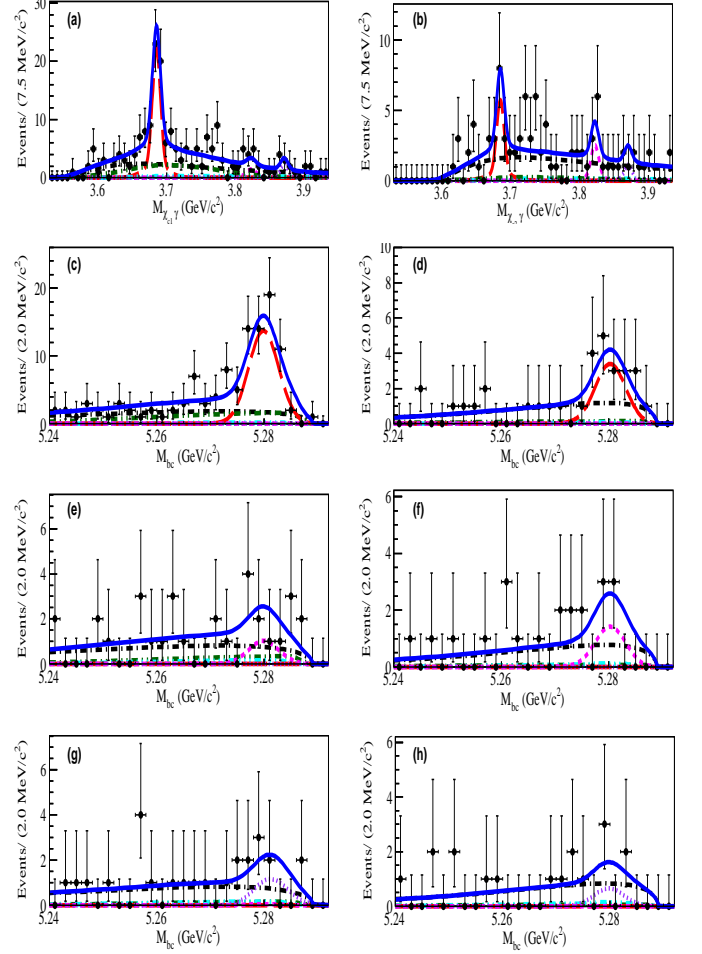


FIG. 3: 2D UML fit projection for  $B^0 \rightarrow (\chi_{c1}\gamma)K_S^0$  decays: (a)  $M_{\chi_{c1}\gamma}$  distribution for  $M_{bc} > 5.27 \text{ GeV}/c^2$ , (b)  $M_{\chi_{c2}\gamma}$  distribution for  $M_{bc} > 5.27 \text{ GeV}/c^2$ , (c)  $M_{bc}$  distribution for  $3.660 \text{ GeV}/c^2 < M_{\chi_{c1}\gamma} < 3.708 \text{ GeV}/c^2$  ( $\psi'$  region), (d)  $M_{bc}$  distribution for  $3.660 \text{ GeV}/c^2 < M_{\chi_{c2}\gamma} < 3.708 \text{ GeV}/c^2$  ( $\psi'$  region), (e)  $M_{bc}$  distribution for  $3.805 \text{ GeV}/c^2 < M_{\chi_{c1}\gamma} < 3.845 \text{ GeV}/c^2$  ( $X(3823)$  region), (f)  $M_{bc}$  distribution for  $3.805 \text{ GeV}/c^2 < M_{\chi_{c2}\gamma} < 3.845 \text{ GeV}/c^2$  ( $X(3823)$  region), (g)  $M_{bc}$  distribution for  $3.84 \text{ GeV}/c^2 < M_{\chi_{c1}\gamma} < 3.89 \text{ GeV}/c^2$  ( $X(3872)$  region) and (h)  $M_{bc}$  distribution for  $3.84 \text{ GeV}/c^2 < M_{\chi_{c2}\gamma} < 3.89 \text{ GeV}/c^2$  ( $X(3872)$  region). The curves used in the fits are described in [33].

results in 0.7 MeV as the  $M_{X(3823)}$  systematic error. In order to estimate the width, we float this parameter and find no sensitivity with the available statistics: the width is  $1.7 \pm 5.5 \text{ MeV}$ . Using pseudo-experiments generated with different width hypotheses for the  $X(3823)$ , the U.L. at 90% C.L. on its width is estimated to be 24 MeV.

The mass of the  $X(3823)$  is near the potential model expectations for the  $1^3D_J$  states' centroid mass: the Cornell [19] and the Buchmüller-Tye [20] potentials give 3810 MeV/ $c^2$ . Other models predict the mass of  $\psi_2$  (the  $1^3D_2$   $c\bar{c}$  state, having  $J^{PC} = 2^{--}$ ) to be 3815-3840 MeV/ $c^2$  [35–37]. The  $X(3823)$  mass agrees quite well

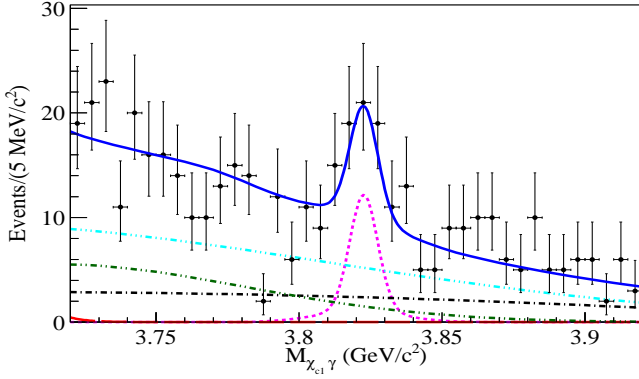


FIG. 4: 2D UML fit projection of  $M_{\chi_{c1}\gamma}$  distribution for the simultaneous fit of  $B^{\pm} \rightarrow (\chi_{c1}\gamma)K^{\pm}$  and  $B^0 \rightarrow (\chi_{c1}\gamma)K_S^0$  decays for  $M_{bc} > 5.27$  GeV/ $c^2$ . The curves used in the fits are described in [33].

TABLE I: Summary of the results. Signal yield ( $Y$ ) from the fit, significance ( $S$ ) with systematics included, corrected efficiency ( $\epsilon$ ) and measured  $\mathcal{B}$ . For  $\mathcal{B}$ , the first (second) error is statistical (systematic). Here, in the neutral  $B$  decay case, the  $K_S^0 \rightarrow \pi^+\pi^-$  branching fraction is included in the efficiency ( $\epsilon$ ) but the factor of 2 (for  $K^0 \rightarrow K_S^0$  or  $K_L^0$ ) is separately taken into account.

Decay	Yield ( $Y$ )	$S(\sigma)$	$\epsilon(\%)$	Branching fraction
$B^{\pm} \rightarrow \psi'(\rightarrow \chi_{cJ}\gamma)K^{\pm}$				$\mathcal{B}(10^{-4})$
$\chi_{c1}$	$193.2 \pm 19.2$	14.8	8.6	$7.7 \pm 0.8 \pm 0.9$
$\chi_{c2}$	$59.1 \pm 8.4$	7.8	6.0	$6.3 \pm 0.9 \pm 0.6$
$B^0 \rightarrow \psi'(\rightarrow \chi_{cJ}\gamma)K^0$				
$\chi_{c1}$	$50.3 \pm 7.3$	7.2	5.1	$6.8 \pm 1.0 \pm 0.7$
$\chi_{c2}$	$12.9 \pm 4.4$	2.9	3.5	$4.7 \pm 1.6 \pm 0.8$
$B^{\pm} \rightarrow X(3823)(\rightarrow \chi_{cJ}\gamma)K^{\pm}$				$\mathcal{B}(10^{-6})$
$\chi_{c1}$	$33.2 \pm 9.7$	3.8	10.9	$9.7 \pm 2.8 \pm 1.1$
$\chi_{c2}$	$0.3 \pm 3.9$	0.1	8.8	$< 3.6$
$B^0 \rightarrow X(3823)(\rightarrow \chi_{cJ}\gamma)K^0$				
$\chi_{c1}$	$3.9 \pm 3.4$	1.2	6.0	$< 9.9$
$\chi_{c2}$	$5.3 \pm 2.9$	2.4	5.0	$< 22.8$
$B^{\pm} \rightarrow X(3872)(\rightarrow \chi_{cJ}\gamma)K^{\pm}$				
$\chi_{c1}$	$-0.9 \pm 5.1$		11.1	$< 1.9$
$\chi_{c2}$	$4.7 \pm 4.4$	1.3	9.3	$< 6.7$
$B^0 \rightarrow X(3872)(\rightarrow \chi_{cJ}\gamma)K^0$				
$\chi_{c1}$	$4.6 \pm 3.0$	1.6	6.2	$< 9.6$
$\chi_{c2}$	$2.3 \pm 2.2$	1.1	5.2	$< 12.2$

with these models. In addition, since no peak has been seen around  $X(3823)$  in the  $D\bar{D}$  final state [38], one expects that  $\psi_2$  does not decay to  $D\bar{D}$  [36]. The ratio  $R_B = \frac{\mathcal{B}(X(3823) \rightarrow \chi_{c2}\gamma)}{\mathcal{B}(X(3823) \rightarrow \chi_{c1}\gamma)} < 0.41$  (at 90% C.L.) is consistent with the expectation ( $R_B \sim 0.2$ ) for  $\psi_2$  [39, 40]. The limited data preclude an analysis of the decay product angular distribution to determine the  $J^{PC}$  assignment of the  $X(3823)$ . The product of branching fractions for the

$X(3823)$  is approximately two orders of magnitude lower than for the  $\psi'$ , as shown in Table I; it is consistent with the interpretation of the  $X(3823)$  as  $\psi_2(1^3D_2)$ , whose production rate is suppressed by the factorization [41] in the two-body  $B$  meson decays.

In summary, we obtain the first evidence of a narrow state,  $X(3823)$ , that decays to  $\chi_{c1}\gamma$  with a mass of  $3823.1 \pm 1.8(\text{stat}) \pm 0.7(\text{syst})$  MeV/ $c^2$  and a significance of  $3.8 \sigma$ , including systematic uncertainties. We measure the branching fraction product  $\mathcal{B}(B^{\pm} \rightarrow X(3823)K^{\pm})\mathcal{B}(X(3823) \rightarrow \chi_{c1}\gamma) = (9.7 \pm 2.8 \pm 1.1) \times 10^{-6}$ . No evidence is found for  $X(3823) \rightarrow \chi_{c2}\gamma$  and we set an U.L. on its branching fraction product  $\mathcal{B}$  as well as the ratio  $R_B \equiv \frac{\mathcal{B}(X(3823) \rightarrow \chi_{c2}\gamma)}{\mathcal{B}(X(3823) \rightarrow \chi_{c1}\gamma)} < 0.41$  at 90% C.L. The properties of the  $X(3823)$  are consistent with those expected for the  $\psi_2(1^3D_2 c\bar{c})$  state. We also determine the U.L. on the product of the branching fractions,  $\mathcal{B}(B^{\pm} \rightarrow X(3872)K^{\pm})\mathcal{B}(X(3872) \rightarrow \chi_{c1}\gamma) < 1.9 \times 10^{-6}$  at 90% C.L.; this is less than one quarter of the corresponding value in  $X(3872) \rightarrow J/\psi\pi^+\pi^-$  [9]. In addition, we obtain constraints for all of the  $\chi_{cJ}\gamma K$  final states in neutral and charged  $B$  decays. Our results show that the  $X(3872)$ 's  $C$ -odd partner production in the two-body  $B$  decays or its decay into  $\chi_{cJ}\gamma$  are found to be considerably suppressed.

We thank the KEKB group for excellent operation of the accelerator; the KEK cryogenics group for efficient solenoid operations; and the KEK computer group, the NII, and PNNL/EMSL for valuable computing and SINET4 network support. We acknowledge support from MEXT, JSPS and Nagoya's TLPSC (Japan); ARC and DIISR (Australia); FWF (Austria); NSFC (China); MSMT (Czechia); CZF, DFG, and VS (Germany); DST (India); INFN (Italy); MEST, NRF, GSDC of KISTI, and WCU (Korea); MNiSW and NCN (Poland); MES and RFAAE (Russia); ARRS (Slovenia); IKERBASQUE and UPV/EHU (Spain); SNSF (Switzerland); NSC and MOE (Taiwan); and DOE and NSF (USA). This work is partly supported by MEXT's Grant-in-Aid for Scientific Research on Innovative Areas ("Elucidation of New hadrons with a Variety of Flavors").

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 where  $\epsilon = \frac{\sigma}{a} + x_p$  and  $\sigma_0 = \frac{\ln(a\sqrt{2\ln 2} + \sqrt{1+2a^2\ln 2})}{\sqrt{2\ln 2}}$ . Here,  $N_0$  is the normalization,  $\sigma$  is the standard deviation,  $x_p$  is the mean and  $a$  is the asymmetry.
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